

Communication

Hybrid Method of Artificial Neural Network and Simulated Annealing Algorithm for Optimizing Wideband Patch Antennas

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Abstract—In order to design the wideband patch antenna, a hybrid method based on the artificial neural network (ANN) and the simulated annealing (SA) algorithm is proposed in this paper. The ANN is employed to describe the nonlinear relationship between the geometric parameters and the S -parameters of the antenna. The ANN is trained by the dataset got by the High Frequency Structure Simulator (HFSS). More importantly, the dataset is divided into three groups according to their own characteristics so that the ANN can be trained faster and better. The SA is employed to broaden the bandwidth of the patch antenna with the required center frequency. Then three wideband patch antennas with different center frequencies are designed to demonstrate the feasibility of the proposed method. Several slots are added to the patch to achieve the wide bandwidth. The results prove that the proposed method can obtain the wideband patch antenna quickly and efficiently.

Index Terms—artificial neural network, simulated annealing algorithm, wideband antenna.

I. INTRODUCTION

With the rapid development of the information technology, spectrum resources are increasingly becoming scarce. As an important part of the communication system, wideband antennas are becoming more and more demanding [1]. In general, the design of the wideband antenna is more time-consuming than that of the narrowband antenna. To speed up the design, many methods such as using parametric study [2], applying various optimization algorithms [3], [4] and employing the artificial neural network (ANN) [5], [6] have been proposed.

As a powerful method, the ANN can learn the complex nonlinear relationship between the input and output after being trained by the dataset. It has contributed greatly to modeling microwave filters [7], power amplifiers [8], [9], transistors

[10] and antenna designs [11]–[14]. The ANN can greatly accelerate the speed of antenna optimization. Therefore, the antenna design based on the ANN has received more and more attention.

The ANN can predict the electromagnetic (EM) responses of the antenna accurately after it is well trained [15], [16]. In [17], a method with the ANN for array synthesis is proposed, where two serial ANNs are employed. One ANN is used as an encoder and the other is used as a decoder to realize the synthesis of the beam pattern for the linear array. In [18], the author utilizes the combination of the ANN and the data classification technology to improve the performance of the antenna.

In addition to above applications, the inverse problems of the antenna design could also be solved by the ANN [19], [20]. The EM responses of the antenna are fed into the ANN, and the geometric parameters could be output by the ANN. In [21], an ANN inverse model is established, in which the EM field intensity is the input, while the output is the radius of the loop antenna. A multi-branch ANN is proposed to improve the performance of antenna arrays in [22]. The dataset is divided into different groups by judging the monotonicity of the data for solving the nonuniqueness problem, and each group is employed to train each branch.

In this paper, a hybrid method applying the combination of the ANN and the simulated annealing (SA) algorithm to design a wideband patch antenna is proposed. The dataset is employed to train the ANN which is obtained from the High Frequency Structure Simulator (HFSS). The input of the ANN is geometric parameters while the output is S -parameters. A trained ANN can describe the relationship between the geometric parameters and the EM responses of the antenna. Additionally, the ANN is called by the SA algorithm to calculate the cost function. Compared to the traditional optimization algorithm, the proposed method does not need to call the electromagnetic simulation repeatedly. As a result, it can speed up the design of the antenna, which requires only a small amount of human resources and can reduce the workload of the designer greatly. More importantly, the characteristic of the dataset is analyzed, and the dataset is separated into three subsets to train the ANN. In this way, the ANN can be trained better and faster. The bandwidth and center frequency of the antennas are optimized simultaneously. Three wideband patch antennas with different center frequencies are designed to verify the validity of the proposed method.

The paper is arranged as follows. The proposed method is introduced in detail in Section II. In Section III, the

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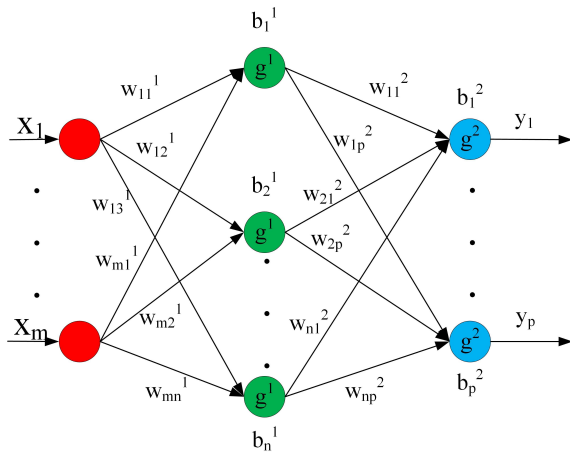


Fig. 1. The ANN with the input layer, one hidden layer and the output layer.

configuration of the antenna, the basic theory of the ANN and the SA algorithm in the proposed method are introduced. In Section IV, the simulated and measured results of the three wideband patch antennas are given. Section V concludes the paper.

II. PROPOSED HYBRID METHOD

A. Artificial Neural Network

As a mathematical model for information processing, the ANN is inspired by biological neural network. Although the ANN requires a large number of parameters and takes too long to learn, it has many advantages at the same time, for example, it can fully approximate complex nonlinear relations, have the ability of associative memory, and high classification accuracy. So the ANN is used to predict the relationship between the geometric parameters and EM responses of the antenna. The structure of a simple ANN with three layers is shown in Fig. 1. The ANN has one input layer, one hidden layer and one output layer, and each layer has some neurons. The weights and thresholds are applied to connect neurons in adjacent layers. The activation functions could introduce nonlinear factors to the ANN, so that it can solve nonlinear problems.

In the ANN, geometric parameters of the antenna are the input, while EM responses of that are the output. x_i represents the i th geometric parameter ($1 \leq i \leq m$), and m is the number of input neurons. y_k indicates the k th EM response ($1 \leq k \leq p$). And p is the number of output neurons. y_k could be calculated by

$$y_k = g_2 \left\{ \sum_{j=1}^n \left[w_{jk}^2 g_1 \left(\sum_{i=1}^m w_{ij}^1 x_i - b_j^1 \right) - b_k^2 \right] \right\} \quad (1)$$

where w_{ij}^1 represents the weight connecting the i th input neuron with j th hidden neuron, and w_{jk}^2 represents the weight which connects the j th hidden neuron with k th neuron in the output layer. b_j^1 indicates the threshold for the j th hidden neuron, while b_k^2 indicates the threshold for the k th output neuron. $g_1(x)$ and $g_2(x)$ are activation functions in the hidden

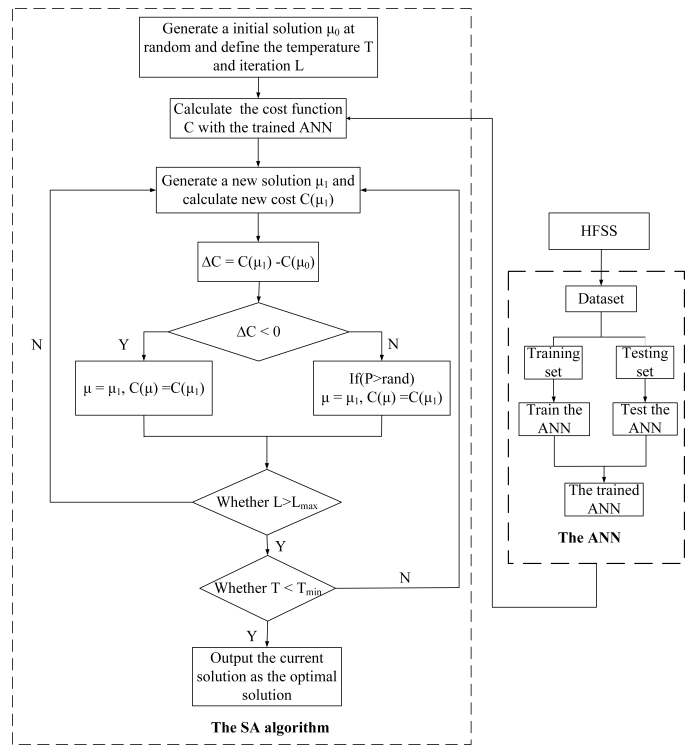


Fig. 2. Flow chart of the proposed hybrid method.

layer and in the output layer, respectively. $g_1(x)$ and $g_2(x)$ can be expressed as

$$g_1(x) = \frac{1}{1 + e^{-x}} \quad (2)$$

$$g_2(x) = x \quad (3)$$

In training the ANN, the error is propagated back by gradient descent method. During the back propagation, the weights and thresholds of the ANN are updated continuously until the error is smaller than the set goal.

B. Simulated Annealing Algorithm

In the proposed method, the key of the SA algorithm is to construct the cost function which can be calculated with the trained ANN. The output of the ANN is taken as part of the cost function. The cost function C is given by

$$C = \omega \frac{f_1}{f_2} + (1 - \omega) \left| \left(\frac{f_1 + f_2}{2f_0} - 1 \right) \right| \quad (4)$$

where f_0 is the center frequency. The bandwidth is from f_1 to f_2 , which are obtained from the ANN. Besides, ω is the weight of the bandwidth whose value is 0.02. In Fig.2, the flow chart of the whole proposed hybrid method is given, which generally consists of the ANN and SA algorithm.

III. WIDEBAND PATCH ANTENNA DESIGN

A. The Structure of the Patch Antenna

The configuration of the patch antenna is given in Fig. 3. The antenna mainly consists of two substrates separated by an air gap. The first substrate is FR4 and the second substrate is

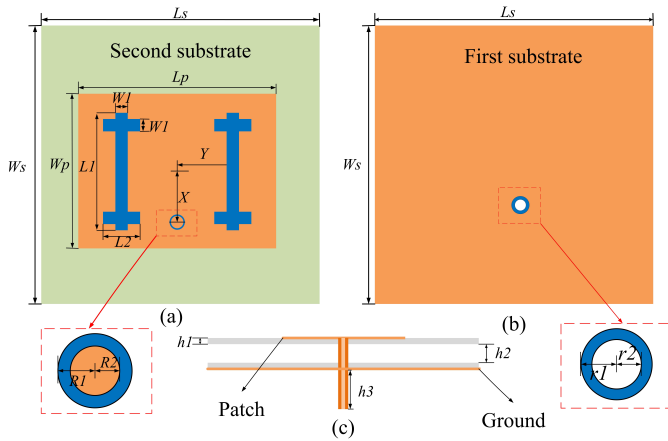


Fig. 3. Configuration of the antenna.(a) Top view. (b) Bottom view. (c) Side view. ($L_s = 52$, $W_s = 52$, $L_p = 26$, $W_1 = 0.65$, $X = 5.2$, $R_1 = 1.43$, $R_2 = 1.3$, $r_1 = 0.74$, $r_2 = 0.32$, $h_1 = 0.508$, $h_2 = 1.71$, $h_3 = 3.9$, unit: mm)

TABLE I
DATASET OF THE PATCH ANTENNA (UNIT:MM)

Geometrical variables	Min	Max	Step
L_1	1	15	2
L_2	0.5	5	0.5
Y	1	9	2
W_p	18.2	23.4	2.6

RO4003. The patch is printed on the second substrate, and two symmetrical cross slots are added on the patch to make the bandwidth increased. The dimensions and placement of the slots and the width of the patch can be changed, while other parameters are fixed. Three wideband antennas with different center frequencies are designed based on the patch antenna. The center frequency of the Antenna 1 is 9 GHz, while those of the Antenna 2 and Antenna 3 are 10 GHz and 11 GHz, respectively.

B. Building the ANN to Predict EM Responses of the Patch Antenna

In order to predict EM responses of the patch antenna, the ANN is built. L_1 , L_2 , Y and W_p are fed into the ANN, and reflection coefficients are output by the ANN. The dataset containing 1200 sets which is produced by HFSS is used to train and test the ANN as shown in the Table I. The dataset is divided into the training set (80%) and the testing set (20%) by random. And all calculations are carried out by an Intel i7-10700 2.90 GHz machine with 32 GB RAM.

Since there are 4 geometric parameters and 41 output frequency points, The input layer of the ANN has 4 neurons, while the output layer owns 41 neurons. Each hidden layer has q neurons, and q is given by

$$q = \sqrt{a + b} + c \quad (5)$$

where a indicates the number of input neurons and b is that of output neurons. c is a random integer from 1 to 10. It can be calculated that q is from 8 to 17. q is determined to be 15 and the number of hidden layers is 3. The learning rate is determined to be 0.001. And the Mean Square Error (MSE)

TABLE II
THE TRAINING EPOCHS, TRAINING TIME AND TESTING ERRORS OF THE ANN_T AND OF THE THREE ANNS

	Training epoch	Training time (minute)	Testing error
ANN_t	3000	50	9.87×10^{-4}
ANN_1	714	7	2.82×10^{-4}
ANN_2	668	6	3.89×10^{-4}
ANN_3	609	5	1.35×10^{-4}

which is utilized to assess the performance of the ANN is given by

$$\text{MSE}(y, y') = \frac{\sum_{i=1}^N (y_i - y'_i)^2}{N} \quad (6)$$

where y is the output of the testing set while y' represents the calculated value of the ANN. And the testing set has N sets of data, where N is equal to 240.

At the beginning, 1200 sets are employed to train and test the ANN_t. However, the ANN_t could not be trained well. The testing results are shown in Fig. 4(a). It is observed that the results of the testing set do not match with the predictions of the ANN_t very well.

Then, the characteristic of the dataset is analyzed, as shown in Fig. 5. As can be seen from the figure, the dataset can be roughly divided into 3 blocks according to W_p . When $W_p=18.2$ mm, it is represented by the circle. When $W_p=20.8$ mm and $W_p=23.4$ mm, they are represented by the cross and triangle, respectively. In most situation, the center frequency f_0 of the antenna decreases as W_p increases which agrees with the theory of the patch antenna.

Therefore, the dataset is divided into three groups according to different values of W_p , and three sub ANNs including ANN_1, ANN_2 and ANN_3 are built. The testing results of the three sub ANNs are shown in Fig. 4(b). The results of the ANN_1, ANN_2 and ANN_3 are better than that of ANN_t. In Table II, the training epochs, training time and testing errors of the ANN_t and the three ANNs are shown. It is observed that dividing the dataset into three groups and using three sub ANNs can obtain better results, faster training speed and higher accuracy. So, it can be seen that the preprocessing of data is beneficial to the learning of the ANN.

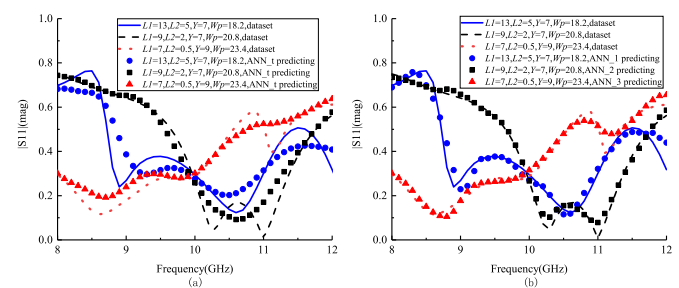


Fig. 4. The results of (a) ANN_t and of (b) ANN_1, ANN_2, ANN_3. Unit:mm.

C. Applying the SA Algorithm to Broaden the Bandwidth of the Patch Antenna with the Required Center Frequency

After the building of the ANNs, the SA algorithm is applied to further broaden the bandwidth of the antennas with the

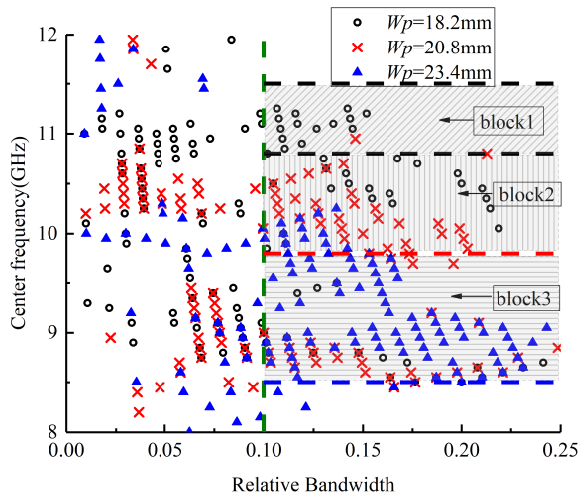


Fig. 5. The result of the data analysis.

required center frequency, because it can avoid the inverse problem in [20]. The required center frequency in the cost function is 9 GHz, 10 GHz and 11 GHz. The minimum value of the cost function is looked for until the SA algorithm stops running. Finally, the three groups of parameters found by the proposed method are shown in Table III. And the simulated results and the calculated results by the proposed method are compared in Fig. 6, which reveals that the simulated results of the three antennas are in a good agreement with the calculated results of the three antennas.

The calculated working frequency band of Antenna 1 is from 7.95 to 10.05 GHz, and the center frequency is 9 GHz, while the simulated bandwidth is from 7.89 to 9.96 GHz, with the center frequency of 8.93 GHz. The calculated bandwidth of Antenna 2 is from 9.15 to 11.05 GHz, and the center frequency is 10.1 GHz. The simulated bandwidth of Antenna 2 is from 9.10 to 11.10 GHz, and the center frequency is 10.1 GHz. The calculated working frequency band of Antenna 3 is from 10.25 to 11.95 GHz, and the center frequency is 11.1 GHz, while the simulated bandwidth is from 10.26 to 11.94 GHz with the center frequency of 11.1 GHz.

The simulated time of the proposed antenna by HFSS is 90 s, whereas the simulated time of the proposed antenna together with the trained ANN is only 0.15 s. It takes about 2000 iterations to optimize the antenna by using the traditional SA algorithm where each iteration needs to call full-wave simulation, so it takes about 50 hours in total. However, by using the proposed method, due to the parallel calculation method, 4 training samples can be calculated at the same time when the simulation software is run. And it takes about 7.5 hours to obtain the 1200 training samples. The total time is 8.16 hours, including training and testing time of the ANN. And only 2 minutes is cost in the optimization of SA. Compared with the traditional SA algorithm calling EM simulations repeatedly during the antenna optimization, the proposed hybrid method can save time and improve the efficiency of antenna design. In addition, the proposed method is compared with the support vector machine (SVM) in terms of required time and prediction accuracy. SVM takes 11.08

TABLE III
THE FINAL VALUES OF THREE PARAMETERS OF THE THREE ANTENNAS

	L1 (mm)	L2 (mm)	Y (mm)	Wp (mm)	Simulated center frequency (GHz)
Antenna 1	9.30	3.12	10.70	18.2	8.93
Antenna 2	19.00	2.43	9.05	20.8	10.1
Antenna 3	11.86	6.45	11.69	23.4	11.1

TABLE IV
THE RUNNING TIME OF THE TRADITIONAL SA ALGORITHM, SVM AND THE PROPOSED HYBRID METHOD

	Time
SA Algorithm	50.63 hours
SVM	7.5 hours (getting dataset) + 11.08 hours (modeling)
Proposed Hybrid Method	8.16 hours (getting dataset and modeling)+ 120 s (optimization)

hours to train and test the 1200 samples with a prediction error of 4.13×10^{-4} , while the proposed method takes 18 minutes in the training and testing, and the average prediction error is 2.69×10^{-4} . The time spent by the traditional SA algorithm, SVM and the proposed method is listed in Table IV.

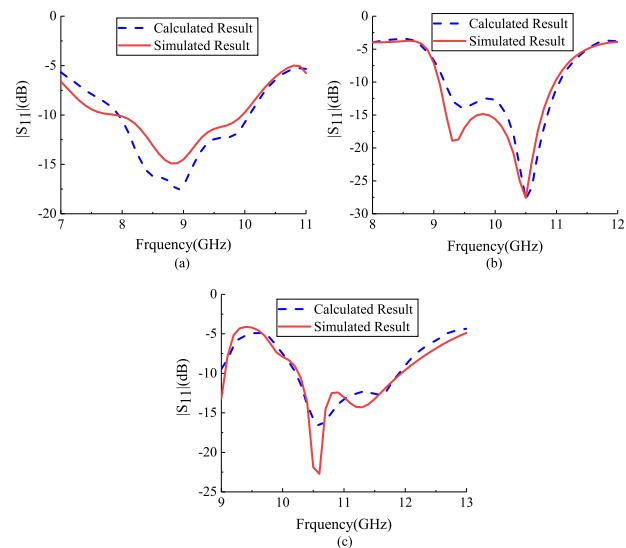


Fig. 6. Calculated and simulated $|S_{11}|$ of (a) Antenna 1, (b) Antenna 2 and (c) Antenna 3.

IV. SIMULATION AND MEASUREMENT

The simulated and measured results of the three antennas obtained from the proposed method are given in this section. The photos of the fabricated antennas are displayed in Fig. 7.

A. Reflection Coefficients

The simulated and measured reflection coefficients of the three antennas are shown in Fig. 8. It can be found that the measured results are in good agreement with the simulated ones. The simulated center frequencies of the three antennas are 8.93 GHz, 10.1 GHz and 11.1 GHz, respectively, while the measured results are 8.8 GHz, 9.85 GHz and 11.2 GHz, respectively. Additionally, the simulated bandwidth of Antenna

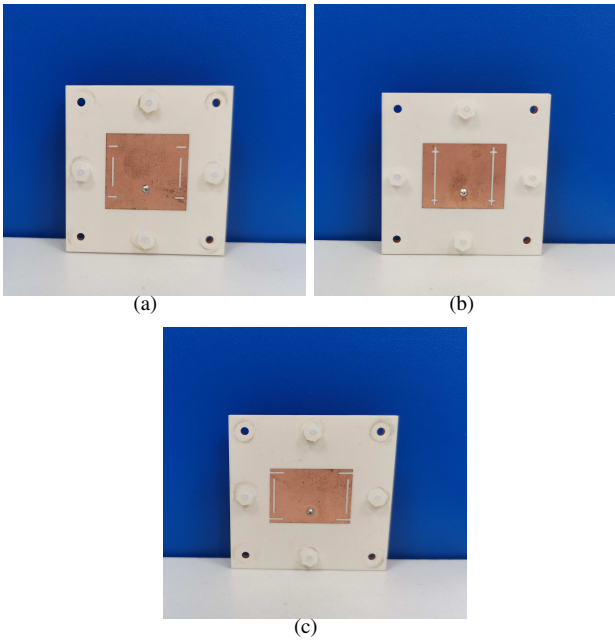


Fig. 7. The photos of (a) Antenna 1, (b) Antenna 2 and (c) Antenna 3.

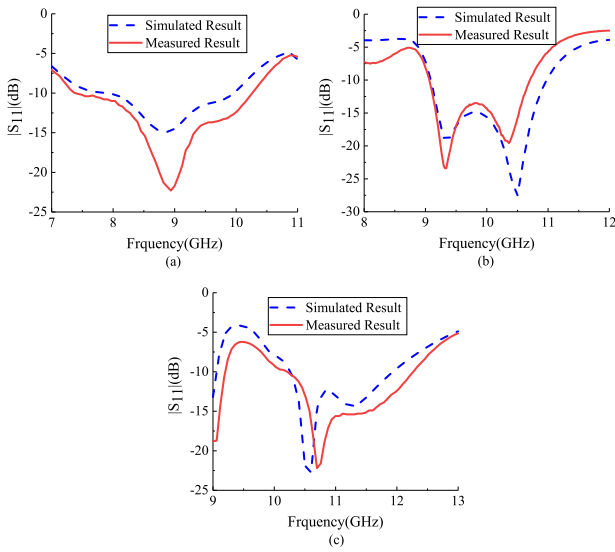


Fig. 8. Simulated and measured $|S_{11}|$ of (a) Antenna 1, (b) Antenna 2 and (c) Antenna 3.

1 is 23.2%, while those of Antenna 2 and Antenna 3 are 19.8% and 15.1%, respectively. The measured bandwidth of the three antennas are 31.8%, 17.3% and 17.9%, respectively.

B. Radiation Patterns and Gains

In Fig. 9, Fig. 10 and Fig. 11, the simulated and measured radiation patterns of the three antennas are given. For each antenna, radiation patterns of two frequencies in the working band are shown. It is observed that the simulated and measured results achieve a good agreement. In addition, in Fig. 12, the simulated and measured gains of three antennas are displayed. It can be found that the measured gains agree with the simulated ones.

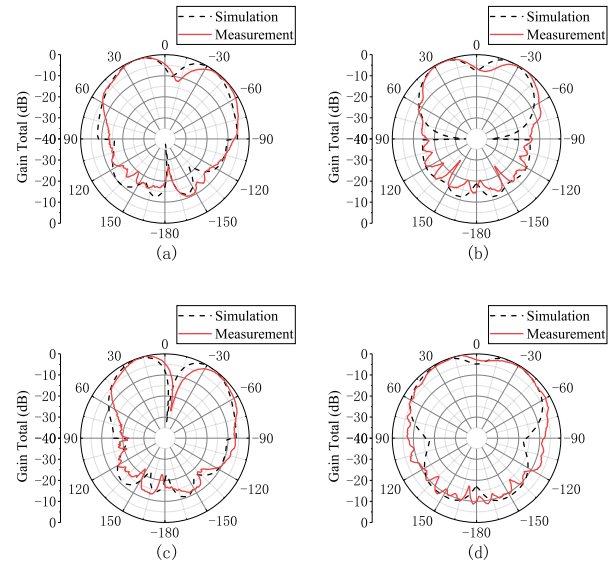


Fig. 9. Simulated and measured radiation patterns of Antenna 1.(a) 8.5 GHz (xoz-plane). (b) 8.5 GHz (yoz-plane). (c) 9 GHz (xoz-plane). (d) 9 GHz (yoz-plane).

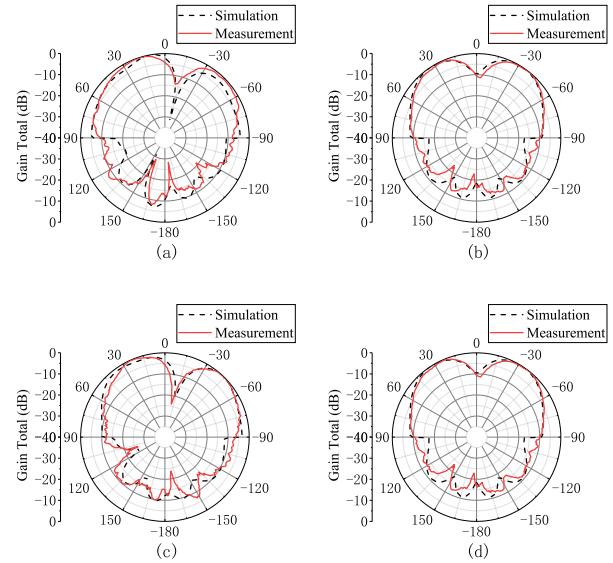


Fig. 10. Simulated and measured radiation patterns of Antenna 2.(a) 9.5 GHz (xoz-plane). (b) 9.5 GHz (yoz-plane). (c) 10 GHz (xoz-plane). (d) 10 GHz (yoz-plane).

V. CONCLUSION

In this paper, a hybrid method applying the ANN and the SA algorithm is proposed to design the wideband patch antenna with the required center frequency. The ANN could describe the nonlinear relationship between the geometric parameters and the EM responses of the antenna after ANN is trained well. The SA algorithm is used to broaden the bandwidth of the antenna with required center frequency. More importantly, three sub ANNs are applied to predict the EM responses of the antenna by data preprocessing. Thus, better results, faster training speed and higher accuracy can be obtained when compared with the ANN trained by the dataset directly. Three

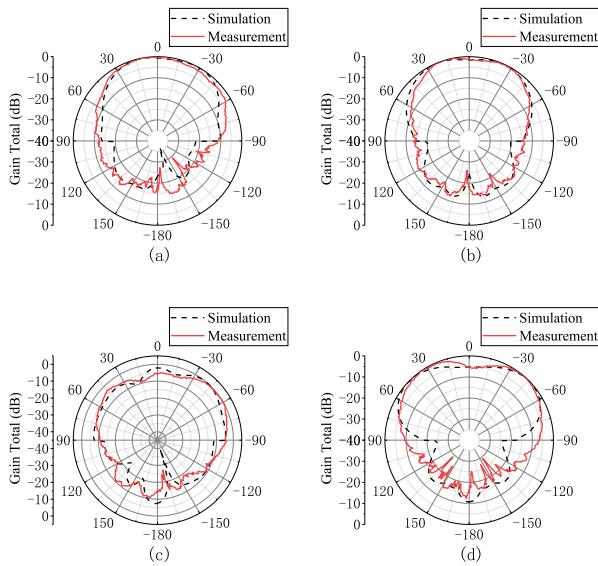


Fig. 11. Simulated and measured radiation patterns of Antenna 3.(a) 10.5 GHz (xoz-plane). (b) 10.5 GHz (yoz-plane). (c) 11 GHz (xoz-plane). (d) 11 GHz (yoz-plane).

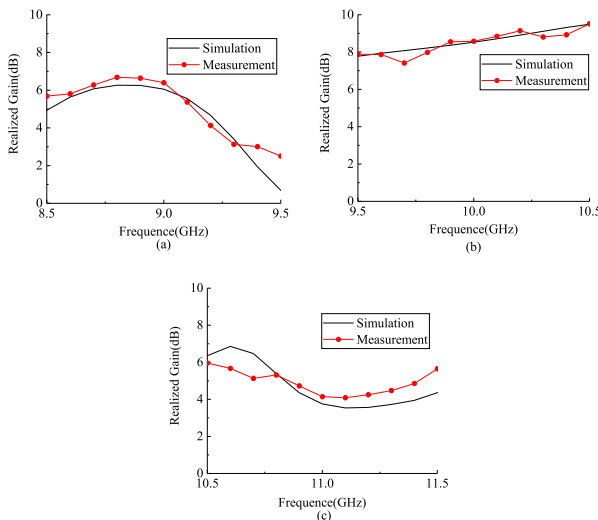


Fig. 12. Simulated and measured gains of (a) Antenna 1, (b) Antenna 2 and (c) Antenna 3.

wideband patch antennas with center frequencies of 8.93 GHz, 10.1 GHz and 11.1 GHz are designed, simulated and fabricated respectively to verify the proposed method. The calculated, simulated and measured results agree well with each other, which proves that the proposed method is effective. The proposed method is promising to design wideband antennas.

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